

NOTE: it does not matter whether the tax is imposed on buyers or sellers; the result will be the same

comp. Eq

$$\begin{aligned} 40 - p &= p \\ 40 &= 2p \\ p &= 20 \end{aligned}$$

$$\begin{aligned} q &= 40 - 20 \\ q &= 20 \end{aligned}$$

**Tax Practice**

I. Demand:  $q = 40 - p$   
Supply:  $q = p$   
Tax = \$10 per unit

Find  $p_d$ ,  $p_s$ ,  $q$ , CS, PS, total welfare, and DWL after the tax. In addition, determine what percentage of the tax is paid by consumers and what percentage of the tax is paid by producers.

TAX REV =  $(10 \times 15) = \$150$

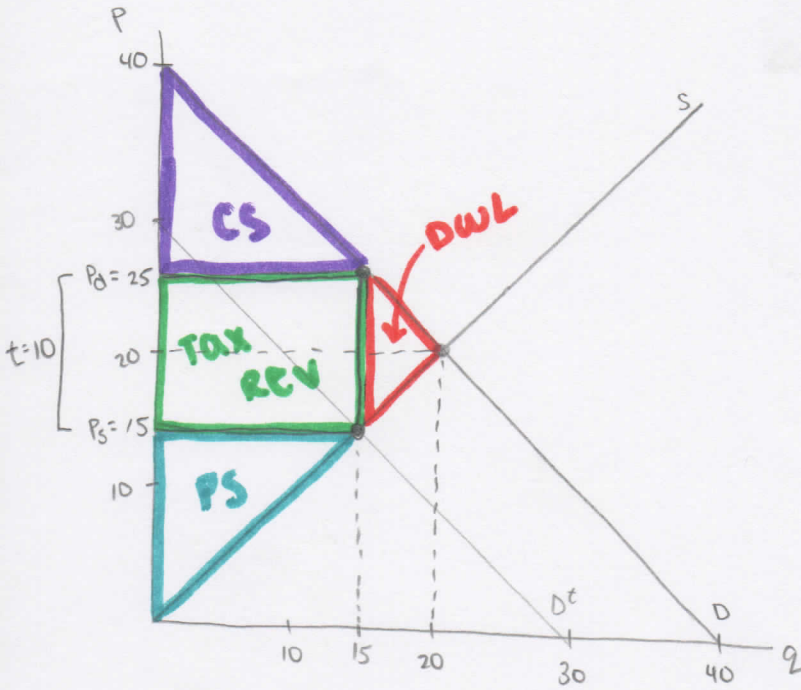
DWL =  $\frac{1}{2}(10)(5) = \$25$

CS =  $\frac{1}{2}(15)(15) = \$112.50$

PS =  $\frac{1}{2}(15)(15) = \$112.50$

Total welfare = CS + PS + TAX REV =  $\$375$

Original equilibrium price = \$20  
Demander's price increases by \$5 after tax; supplier's price falls by \$5  
Demanders:  $\frac{\$5}{\$10} \rightarrow 50\%$  pay  
Suppliers:  $\frac{\$5}{\$10} \rightarrow 50\%$  pay



METHOD 1: Shift Demand

Demand  $\rightarrow$  Inverse  $\rightarrow$  Shift down by tax  
 $q = 40 - p \rightarrow p = 40 - q \rightarrow p = 40 - q - 10$   
 $p = 30 - q$

Find intersection of shifted demand & supply

$30 - q = q$

$30 = 2q$

$q = 15$

Plug  $q$  to inverse demand  $\rightarrow P_d$

$p = 40 - 15$

$P_d = 25$

Plug  $q$  to supply  $\rightarrow P_s$

$P_s = 15$

METHOD 2:  $P_d - t = P_s$

$P_d = 40 - q \quad P_s = q$

$40 - q - t = q$

$40 - q - 10 = q$

$30 - q = q$

$q = 15$

Plug  $q$  to inverse demand

$\rightarrow P_d$

$P_d = 25$

Plug  $q$  to supply

$\rightarrow P_s$

$P_s = 15$

II. Inverse demand:  $p = 18 - 0.5q$   
 Supply:  $q = 4p - 12$   
 Tax = \$6 per unit

Find  $p_d$ ,  $p_s$ ,  $q$ , CS, PS, total welfare, and DWL after the tax. In addition, determine what percentage of the tax is paid by consumers and what percentage of the tax is paid by producers.

Demand:  $q = 36 - 2p$   
 Inverse supply:  $p = \frac{q}{4} + 3$

comp Eq:  
 $36 - 2p = 4p - 12$   
 $48 = 6p$   
 $p = 8$   
 $q = (4 \times 8) - 12$   
 $q = 20$

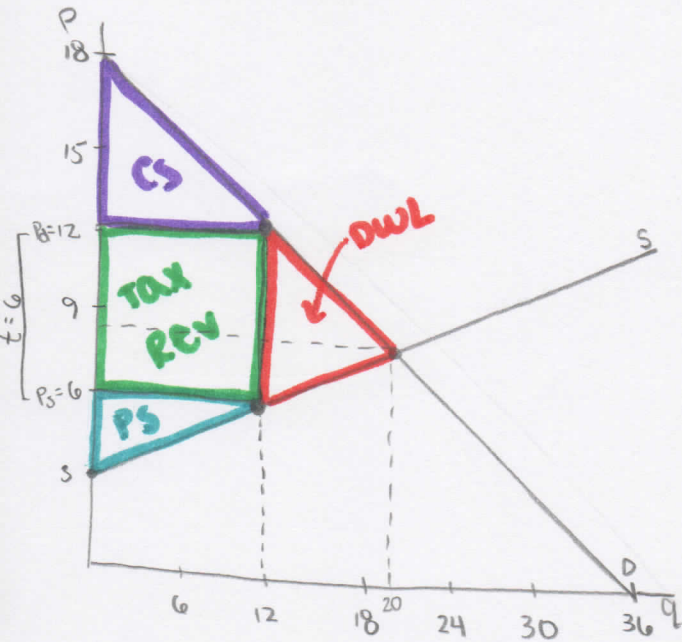
Tax Rev =  $(6 \times 12) = \boxed{\$72}$

DWL =  $\frac{1}{2} (6)(8) = \boxed{\$24}$

CS =  $\frac{1}{2} (6)(12) = \boxed{\$36}$

PS =  $\frac{1}{2} (3)(12) = \boxed{\$18}$

Total welfare = CS + PS + Tax Rev =  $\boxed{\$126}$



original equilibrium price = \$8  
 demander's price increases by \$4  
 after tax; supplier's price falls by \$2

$P_d - t = P_s$

$P_d = 18 - \frac{q}{2}$

$P_s = \frac{q}{4} + 3$

$18 - \frac{q}{2} - 6 = \frac{q}{4} + 3$

$q = \frac{3q}{4}$

$q = 12$

plug  $q$  to inverse supply

$\rightarrow P_s$

$P = \frac{1}{4}(12) + 3$

$P_s = 6$

plug  $q$  to inverse demand

$\rightarrow P_d$

$p = 18 - \frac{1}{2}(12)$

$P_d = 12$

demander's pay:  $\frac{\$4}{\$6} \rightarrow \boxed{66.7\%}$

supplier's pay:  $\frac{\$2}{\$6} \rightarrow \boxed{33.3\%}$

III. Demand:  $q = 5 - p$  Inverse:  $p = 5 - q$   
 Inverse Supply:  $p = 3q - 3$  SUPPLY:  $q = \frac{p}{3} + 1$   
 Tax = \$1 per unit

Find  $p_d$ ,  $p_s$ ,  $q$ , CS, PS, total welfare, and DWL after the tax. In addition, determine what percentage of the tax is paid by consumers and what percentage of the tax is paid by producers.

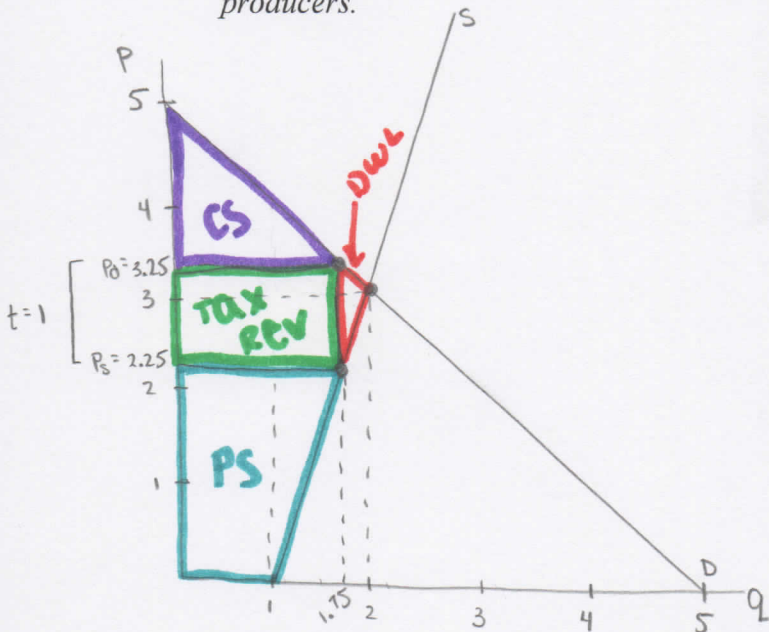
Comp.  
 Eq.

$$5 - q = 3q - 3$$

$$8 = 4q$$

$$q = 2$$

$$p = 5 - 2 \rightarrow p = 3$$



$$\text{TAX REV} = (1 \times 1.75) = \boxed{\$1.75}$$

$$\text{DWL} = \frac{1}{2} (1) (0.25) = \boxed{\$0.125}$$

$$\text{CS} = \frac{1}{2} (1.75) (1.75)$$

$$= \boxed{\$1.53}$$

$$\text{PS} = (2.25 \times 1) + \frac{1}{2} (2.25) (0.75)$$

$$= \boxed{\$3.09}$$

$$\text{Total welfare} = \text{CS} + \text{PS} + \text{TAX REV} = \boxed{\$6.37}$$

original Equilibrium price = \$3

demanders' price increases by \$0.25 after tax; supplier's price falls by \$0.75

$$\text{Demanders' pay} : \frac{\$0.25}{\$1} \rightarrow \boxed{25\%}$$

$$\text{Suppliers' pay} : \frac{\$0.75}{\$1} \rightarrow \boxed{75\%}$$

$$p_d - t = p_s$$

$$p_d = 5 - q$$

$$p_s = 3q - 3$$

$$5 - q - 1 = 3q - 3$$

$$7 = 4q$$

$$q = 1.75$$

Plug  $q$  to inverse demand  
 $\rightarrow p_d$

$$p = 5 - 1.75$$

$$p_d = 3.25$$

Plug  $q$  to inverse supply  
 $\rightarrow p_s$

$$p_s = 3(1.75) - 3$$

$$p_s = 2.25$$